

# RELATIVITY MTH6132

## PROBLEM SET 4

HAND IN ONLY THE STARRED QUESTIONS.

1) A stationary particle of rest mass  $M$  decays into two particles that both move along the  $x$ -axis. One has a rest-mass  $m_1$  and a speed  $u_1$  and the other has a rest-mass  $m_2$  and a speed  $u_2$ . Prove that

$$M^2 = m_1^2 + m_2^2 + 2m_2^2 \frac{u_2}{1 - u_2^2} \left( \frac{1}{u_1} + u_2 \right)$$

2\*) An atom of rest mass  $m_0$  at rest in a laboratory absorbs a photon of frequency  $\nu$ . Use the conservation law of 4-momentum to find the velocity and rest mass of the resulting particle.

3) A particle of rest mass  $m_1$  moving with velocity  $u_1$  along the  $x$ -axis collides with a stationary particle of rest mass  $m_2$  stationary along the  $x$ -axis. If subsequently the particle with rest mass  $m_1$  moves in the direction making an angle of  $60^\circ$  relative to the  $x$ -axis (in the  $x - y$  plane), show that

$$E_1 E_1' (u_1 u_1' - 2) = 2m_2 (E_1' - E_1) - 2m_1^2,$$

where  $E_1$  and  $E_1'$  are the total energies of the particle  $m_1$  before and after the collision respectively and  $u_1'$  is its speed after the collision. [The total energy  $E$  of a particle of rest mass  $m$  and 3-velocity  $\underline{v}$  is  $m\gamma(v)$ .]

4\*) A particle moving along the  $x$ -axis with speed  $v$  disintegrates into two photons (particles with zero rest mass) moving in directions making angles  $\alpha$  and  $\beta$  with the  $x$ -axis and on opposite sides of it. Show that

$$v = \frac{\sin \beta \cos \alpha + \sin \alpha \cos \beta}{\sin \alpha + \sin \beta}$$

[**General hint:** Proceed by writing down the 4-momenta for the particles and photons before and after and using the conservation law of 4-momentum. See notes. ]

**To be placed in the BLUE BOX on 2nd floor of the Maths building by Wednesday 2nd November, 6:00 pm.**

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