

# **King's College London**

**UNIVERSITY OF LONDON**

This paper is part of an examination of the College counting towards the award of a degree. Examinations are governed by the College Regulations under the authority of the Academic Board.

## **B.Sc. EXAMINATION**

**CP1600 Physical Basis of Astronomy**

**Summer 2006**

**Time allowed: THREE Hours**

Candidates should answer **ALL** parts of SECTION A,  
and no more than **TWO** questions from SECTION B.  
No credit will be given for answering further questions.

The approximate mark for each part of a question is indicated in square brackets.

You must not use your own calculator for this paper.  
Where necessary, a College calculator will have been supplied.

**TURN OVER WHEN INSTRUCTED**  
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## Physical Constants

Permittivity of free space	$\epsilon_0$	=	$8.854 \times 10^{-12}$	$\text{F m}^{-1}$
Permeability of free space	$\mu_0$	=	$4\pi \times 10^{-7}$	$\text{H m}^{-1}$
Speed of light in free space	$c$	=	$2.998 \times 10^8$	$\text{m s}^{-1}$
Gravitational constant	$G$	=	$6.673 \times 10^{-11}$	$\text{N m}^2 \text{kg}^{-2}$
Elementary charge	$e$	=	$1.602 \times 10^{-19}$	C
Electron rest mass	$m_e$	=	$9.109 \times 10^{-31}$	kg
Unified atomic mass unit	$m_u$	=	$1.661 \times 10^{-27}$	kg
Proton rest mass	$m_p$	=	$1.673 \times 10^{-27}$	kg
Neutron rest mass	$m_n$	=	$1.675 \times 10^{-27}$	kg
Planck constant	$h$	=	$6.626 \times 10^{-34}$	J s
Boltzmann constant	$k_B$	=	$1.381 \times 10^{-23}$	$\text{J K}^{-1}$
Stefan-Boltzmann constant	$\sigma$	=	$5.670 \times 10^{-8}$	$\text{W m}^{-2} \text{K}^{-4}$
Gas constant	$R$	=	8.314	$\text{J mol}^{-1} \text{K}^{-1}$
Avogadro constant	$N_A$	=	$6.022 \times 10^{23}$	$\text{mol}^{-1}$
Molar volume of ideal gas at STP		=	$2.241 \times 10^{-2}$	$\text{m}^3$
One standard atmosphere	$P_0$	=	$1.013 \times 10^5$	$\text{N m}^{-2}$
Radius of Sun	$R_\odot$	=	$6.961 \times 10^8$	m
Mass of Sun	$M_\odot$	=	$1.989 \times 10^{30}$	kg
Surface Temperature of Sun	$T_\odot$	=	5800	K
Wavelength of maximum flux (Sun)	$\lambda_{\text{MAX}}(\odot)$	=	5500	Å
Solar bolometric magnitude	$M_{\text{bol},\odot}$	=	+4.75	
V filter zero point	$F_\lambda(V=0)$	=	$3.64 \times 10^{-12}$	$\text{W m}^{-2} \text{\AA}^{-1}$
V filter central wavelength	$\lambda_0(V)$	=	5500	Å
V filter bandwidth	$\Delta\lambda(V)$	=	890	Å

**SECTION A – Answer ALL parts of this section**

- 1.1) Define the sidereal and synodic period of a planet. Derive the relation between the sidereal period ( $P$ ) of a superior planet as a function of the synodic period ( $S$ ) and the period ( $E$ ) of the Earth's orbit.

[6 marks]

- 1.2) Define twilight and list the three standard choices of twilight. Why does twilight last longer at higher latitudes? How long does twilight last on the Moon?

[6 marks]

- 1.3) Consider a star with an apparent magnitude  $m_V = 11$ .

Show that we receive a flux of  $400 \text{ photons s}^{-1}\text{m}^{-2} \text{\AA}^{-1}$  from this star. A telescope with a 50 cm aperture has a total throughput  $T_V = 0.3$  in the V band. It uses a CCD detector with quantum efficiency of 80% and you may assume that the contribution to the noise from the sky, read noise and dark current are negligible. Calculate the signal to noise ratio after an exposure of 2 seconds.

[10 marks]

- 1.4) Define hydrostatic equilibrium. Write down the equation of hydrostatic equilibrium.

Consider a star with a constant density  $\rho_0$ . Find the central pressure ( $p$  at  $r = 0$ ) as a function of the stellar mass  $M$  and radius  $R$ .

[10 marks]

- 1.5) For the three observatories at the latitudes listed below, draw a celestial sphere with the zenith, celestial pole, celestial equator and horizon. For each one show a star with hour angle  $H = 0$  hours and declination  $\delta = +45^\circ$ .

a) Latitude  $\phi = 45^\circ\text{N}$

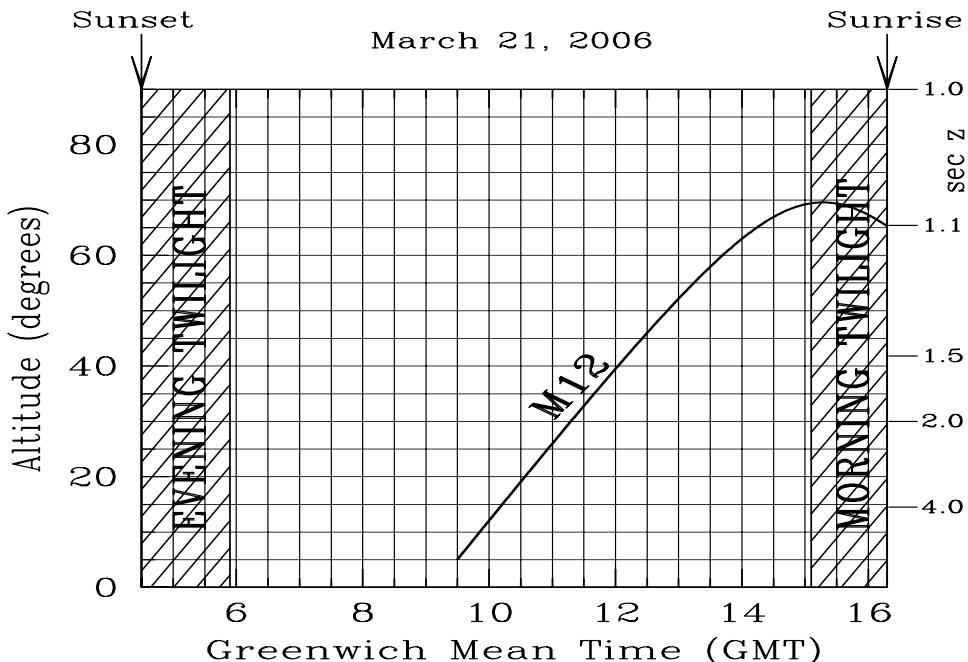
b) Latitude  $\phi = 45^\circ\text{S}$

c) Latitude  $\phi = 80^\circ\text{N}$

[8 marks]

## SECTION B – Answer TWO questions

- 2) The figure below shows the altitude of M12 (which is a globular cluster) above the horizon throughout the night of the 21st of March at some observatory in the Northern hemisphere. The equatorial coordinates of M12 are RA=16h47m and Dec= $-01^{\circ}57'$ .



- a) Determine the latitude and longitude of the observatory, assuming the equation of time is zero.  
[6 marks]
- b) What is the local sidereal time at midnight?  
[4 marks]
- c) The figure shows that March 21st is not the best of days to observe the target. Estimate the ideal **date** to observe M12.  
[5 marks]
- d) A globular cluster is an old stellar population: a system of stars all formed at the same time, about  $10^{10}$  years ago. Why are there no massive stars in M12? Show in a Hertzsprung-Russell diagram the following stellar phases: low-mass main sequence, red giant branch, horizontal branch, and white dwarf. Briefly explain the stellar structure of these phases.  
[10 marks]
- e) Explain why the secant of the zenith angle ( $\sec z$ ) is important when computing atmospheric extinction.  
[5 marks]

- 3) Consider a spaceship on a circular orbit with radius 1 AU around a star with mass  $2M_{\odot}$ .
- Find the period of the circular orbit described above. [5 marks]
  - The effective potential is  $\phi(r) = \lambda^2/2r^2 - GM/r$ . What is meant by effective potential? Describe the meaning of both terms in  $\phi(r)$ . Sketch the effective potential as a function of radius and identify the circular, elliptical, parabolic and hyperbolic orbits. [5 marks]
  - Show that, for any elliptical orbit, the radial component of the velocity  $dr/dt$  is zero only at its aphelion and perihelion. [5 marks]
  - A rocket is fired so that the tangential velocity of the spaceship is increased by 10%. Determine the new orbit by calculating its new semi-major axis and eccentricity. Explain **qualitatively** what would happen if the rocket decreases the tangential velocity of the spaceship by 10%. [10 marks]
  - Consider the initial circular orbit. There is a sudden mass loss process in the star so that its mass instantaneously drops to some value  $M'$  and the spaceship's orbit becomes parabolic (only because of this mass loss). Determine  $M'$ . [5 marks]

P.S. The orbit of a body in a gravitational field can be written in polar coordinates as:  $r = r_0/(1 + \epsilon \cos \theta)$ , where  $\epsilon$  is the eccentricity, which relates the semi-major ( $a$ ) and the semi-minor ( $b$ ) axes of the orbit by  $b^2 = a^2(1 - \epsilon^2)$ . The semi-latus rectum  $r_0$  defines the size of the orbit, and can be written in terms of the angular momentum per unit mass of the orbiting body –  $\lambda = v_{\perp}r$  – and the mass of the star:  $r_0 = \lambda^2/GM$ . It is also related to the semi-major axis by:  $r_0 = a(1 - \epsilon^2)$ .

- 4.a) Define absolute magnitude. Show that a star with absolute magnitude in the V band  $M_V$ , at a distance  $d$  (in parsec) has an apparent magnitude given by:

$$m_V = M_V + 5 \log(d) - 5.$$

[5 marks]

- b) Define Wien's law. Calculate the surface temperature of an A-type star by comparing its wavelength of maximum emission  $\lambda_{MAX}(A) = 3200 \text{ \AA}$ , with that of the Sun.

[5 marks]

- c) An A-type star with apparent magnitude  $m_V = 15.60$  is located 100 pc away. Calculate its absolute magnitude.

The bolometric correction for this type of star is  $-0.2$ . Calculate its radius as a fraction of the solar radius  $R_\odot$ , and identify the type of star.

[10 marks]

- d) Consider the following two A-type stars: Vega ( $m_V = 0.0$ , annual parallax  $0.123''$ ) and Deneb ( $m_V = +1.25$ , distance 490 pc). Compute the ratio of the **observed** fluxes. Compute the ratio of luminosities and radii, assuming they have the same surface temperature and the same bolometric correction.

Determine the radius of Vega in units of  $R_\odot$ , the radius of the Sun. Explain briefly whether Vega and Deneb are main sequence or giant stars.

[10 marks]